

Wavefront Correction

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Iris AO, Inc.



Outline

- Overview of Wavefront Correctors
- Specifications
- Types of DMs
- Fitting Errors
- MEMS DMs: Teaser for the Next Lecture

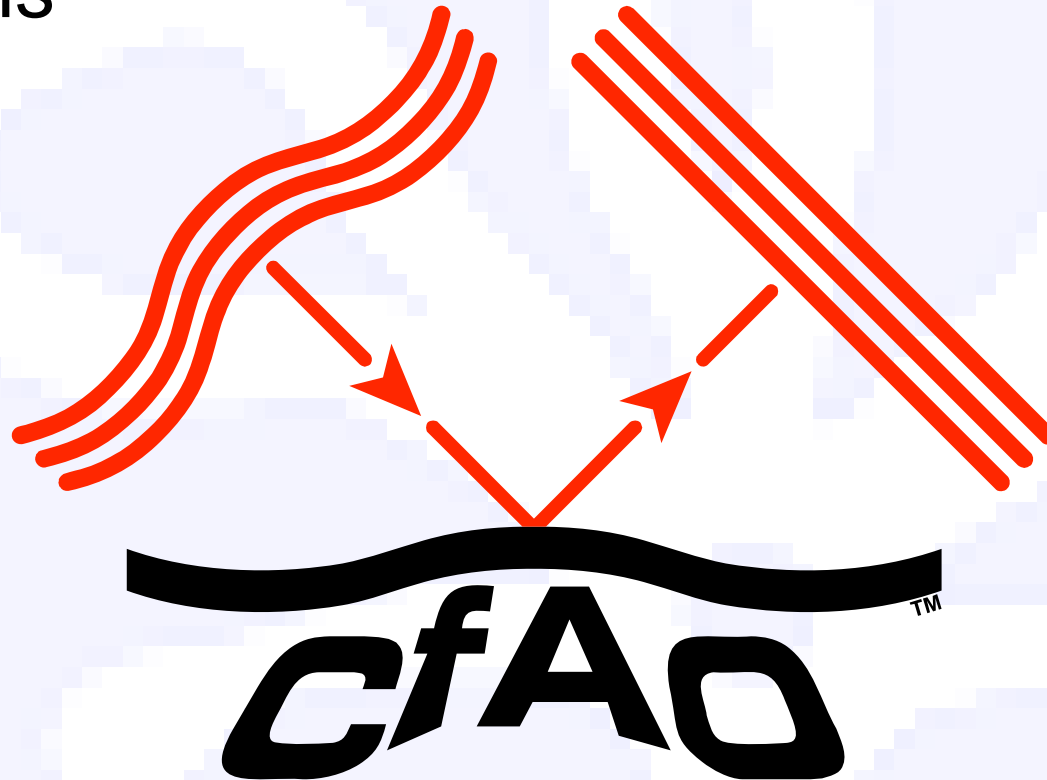


Wavefront Correctors

- Wavefront Corrector: Any device that corrects wavefront distortions
 - Simplest form: eye glasses
 - Modal, low order, static
 - Time-varying distortions
 - **phase**, intensity, polarization, or direction
 - High spatial frequencies
- Spatial Light Modulator: Transducer that modulates incident light
 - Electrical or optical input

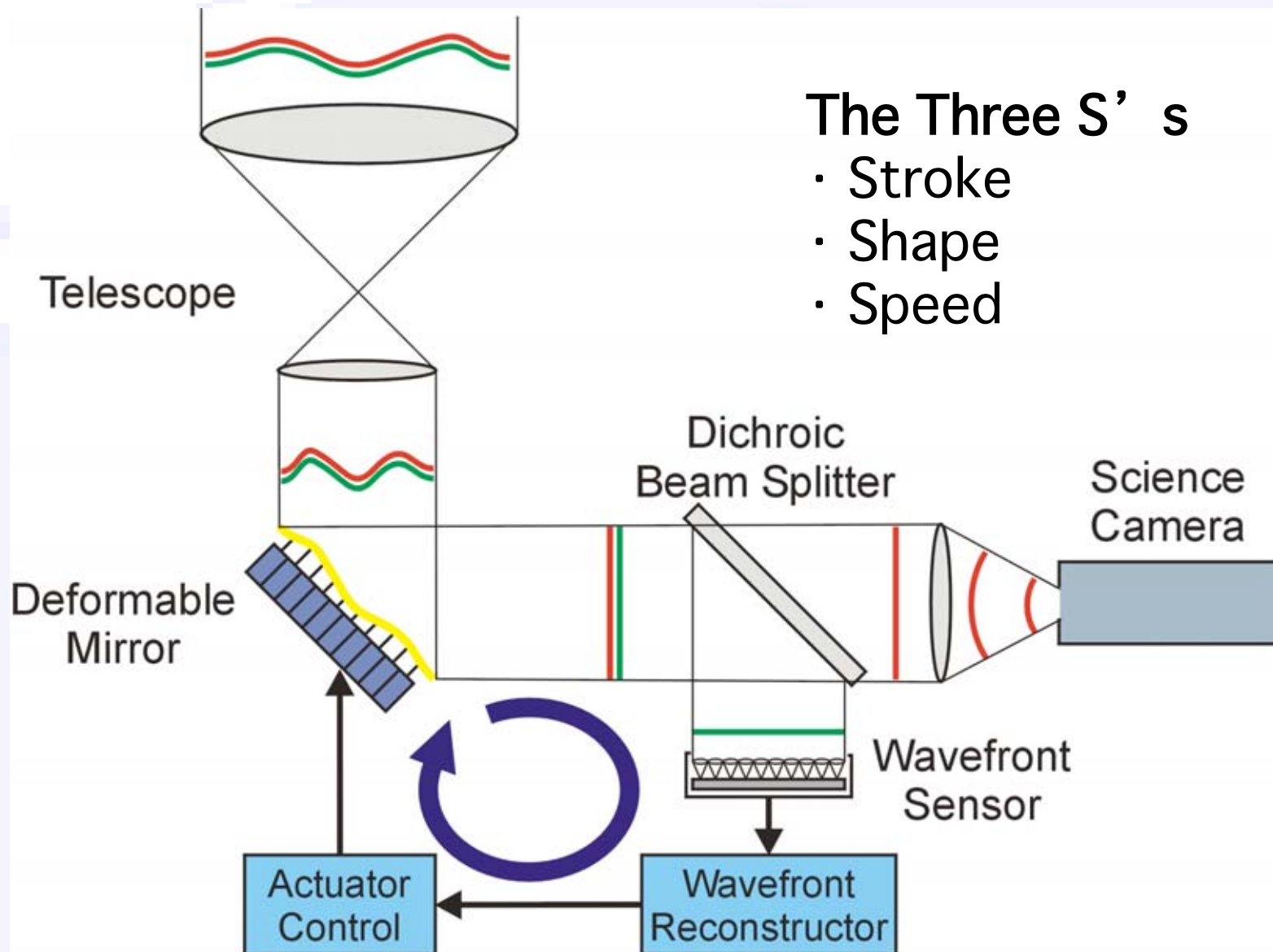
The Deformable Mirror

- Deformable mirrors (DM) physically change shape to correct time-varying wavefront *phase* aberrations





AO System Diagram (Astronomy)



The Three S' s

- Stroke
- Shape
- Speed

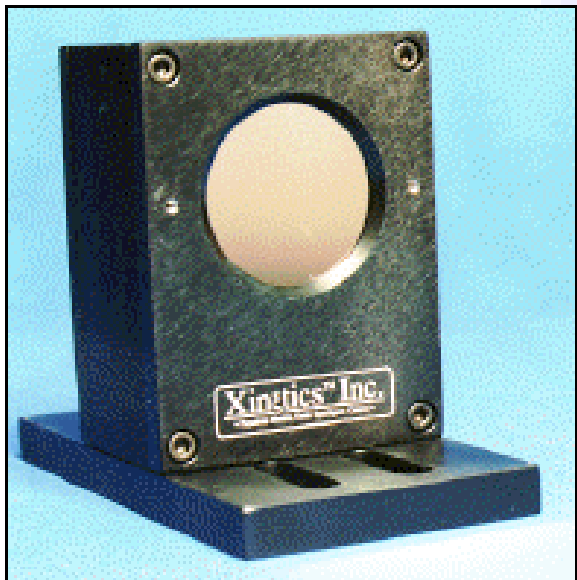
Typical DM Requirements

	Astronomy (10m)	Vision Science
Stroke	5 μm	10-20 μm
Number of Actuators* (Shape)	350-2500 $DOF \propto \left(\frac{D}{r_0}\right)^2$	40-100
Frequency Response (Speed)	1-5 kHz	50-200 Hz
Fill Factor	98%	98%
Mirror-Surface Errors (<i>rms</i>)	30 nm	30 nm
Aperture Size	1-15 cm	3-9 mm

* Continuous mirror with piston actuators

Equations from John W. Hardy, *AO for Astronomical Telescopes*

DMs: *All Shapes and Sizes*



Xinetics Website



Hamamatsu LC-SLM



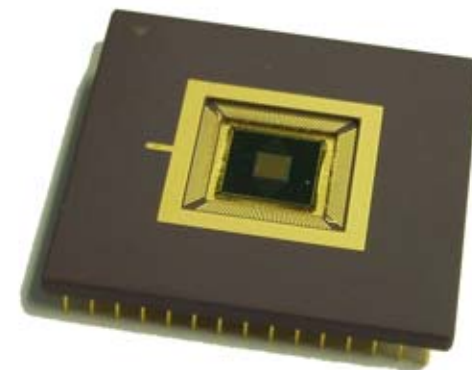
AOptix Bimorph



OKO membrane mirror



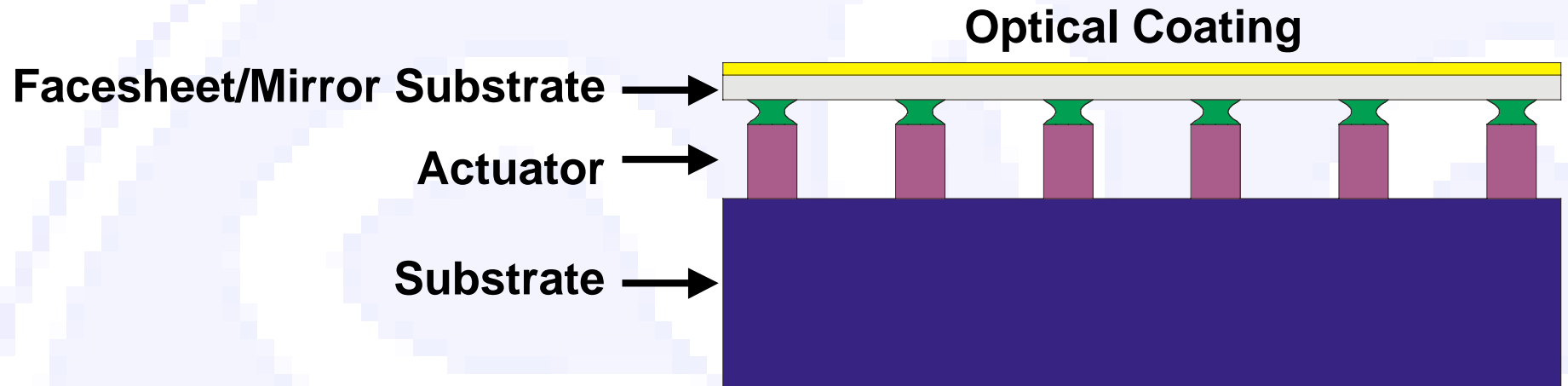
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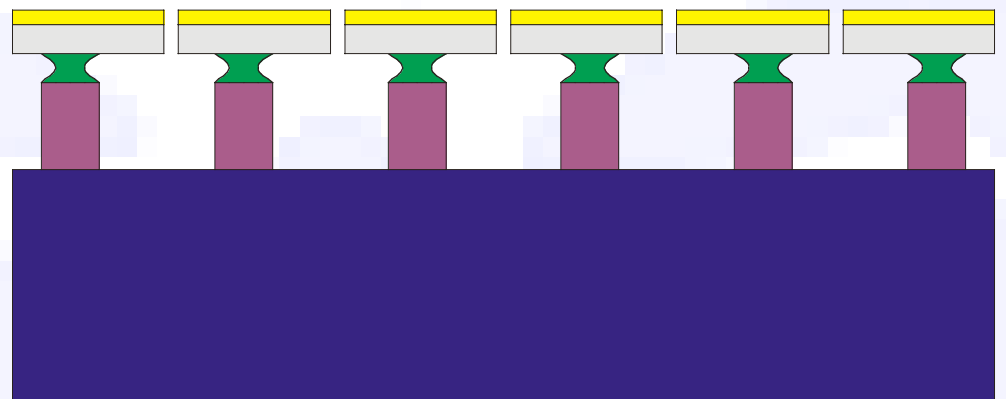
Boston
Micromachines
Corp.

DM Construction

Continuous Facesheet DM



Segmented DM





DM Actuation Methods

Most Common Types

- **Piezoelectric**
 - Strain \propto Electric field
 - +High forces
 - - High voltage $\sim 300V$
 - - Hysteresis
- **Electrostatic**
 - Force \propto Voltage²
 - +Low power
 - - Forces weak for large gaps

Less Common Types

- **Magnetic**
 - Force \propto Current
 - +High forces
 - - High current ($\sim 1A$)/power
- **Thermal**
 - Strain \propto Temperature
 - + High forces
 - - High temperature/power
- **Other Potential Actuators**
 - Pressure
 - Material Phase Change

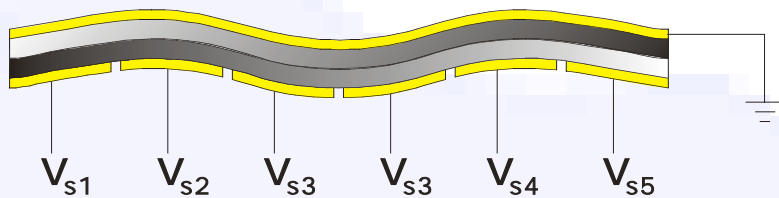
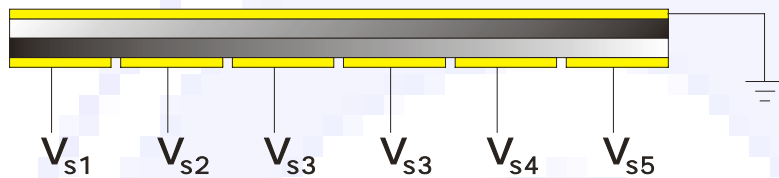


DM Actuation Classes

- Modal
 - Actuators change curvature locally
 - Stroke depends greatly on adjacent actuators
 - Strong influence function between actuators
 - Displacement between actuators is small
 - Stroke \propto actuator-length²
- Zonal
 - Arrays of actuators that push/pull on the mirror
 - Stroke “independent” of adjacent actuators
 - Weak influence function between actuators

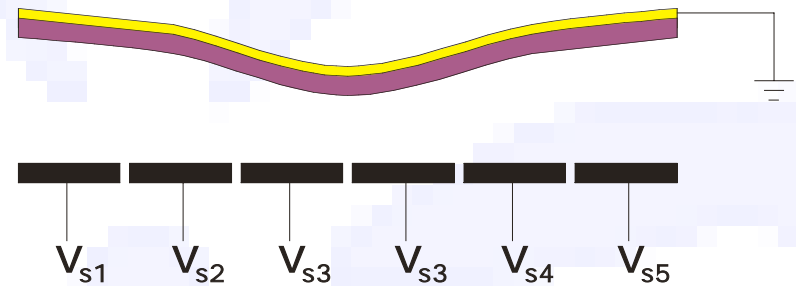
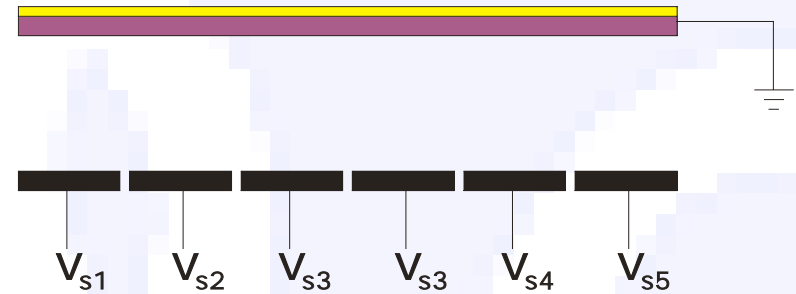
Modal Mirrors

Bimorph Mirror



$$\nabla^2 z \mu \frac{-V(x, y)d_{31}}{t^2}$$

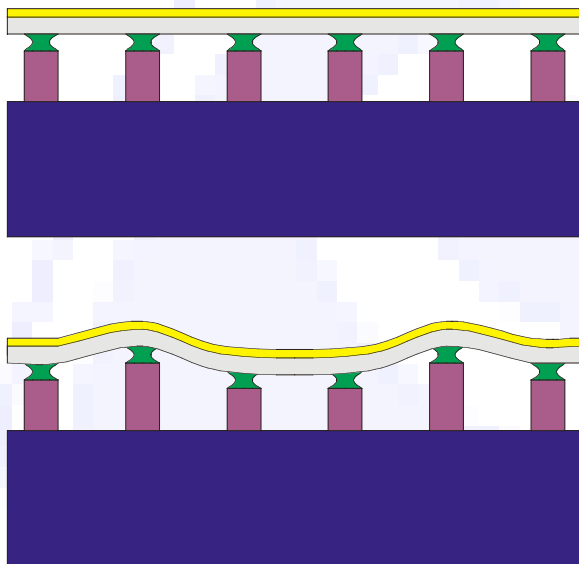
Membrane Mirror



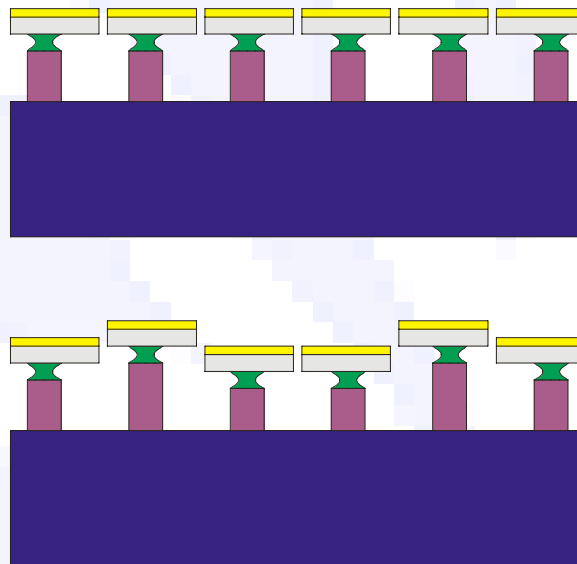
$$\nabla^2 z \mu \frac{-\epsilon_0 V^2}{d^2 \sigma_m}$$

Zonal Mirrors

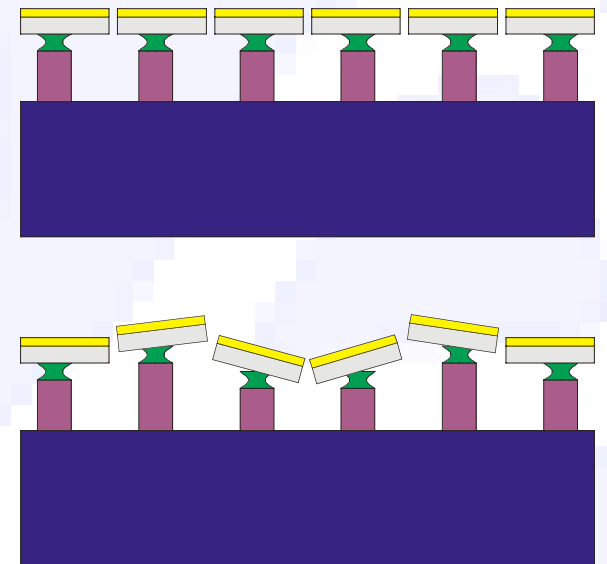
**Continuous
Face Sheet**



**Segmented:
Piston**



**Segmented:
Piston/Tip/Tilt**

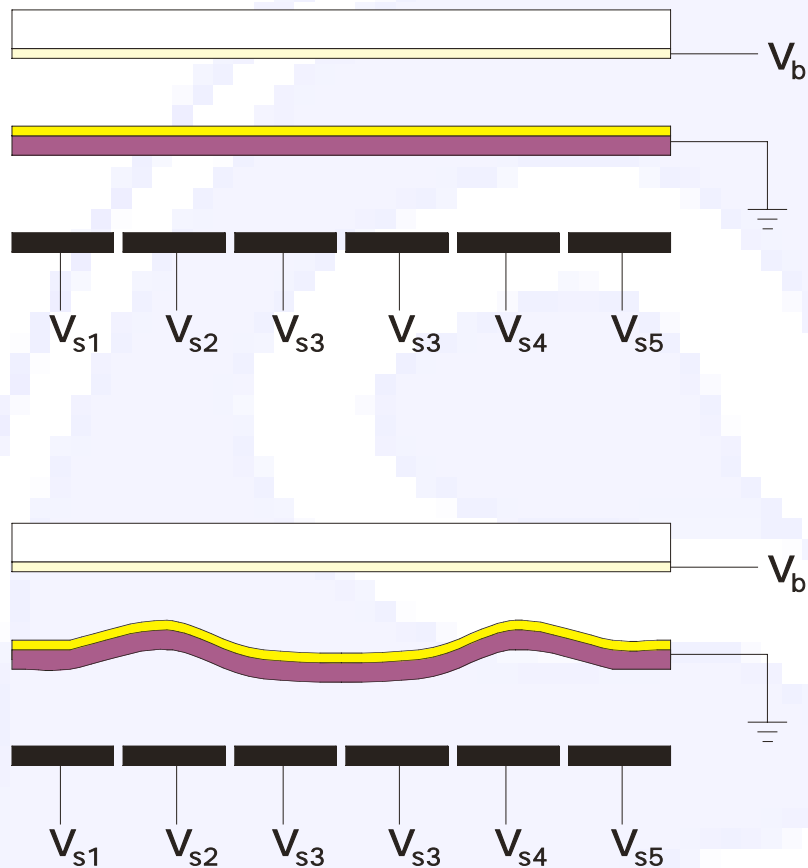


$$z(x, y) \mu V^n$$

$$n=1-2$$

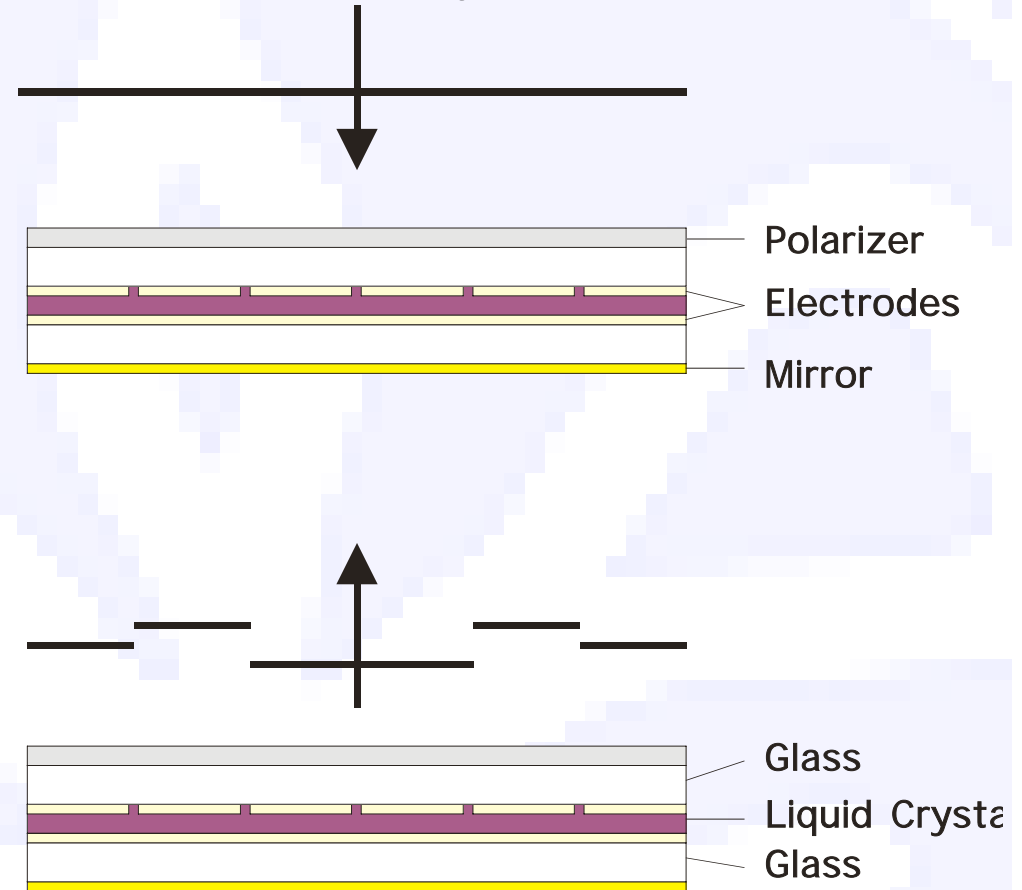
Zonal Mirrors/SLM

Balanced Membrane Mirror



$$z(x, y) \propto V^n \quad n=1-2$$

Liquid-Crystal SLM



$$\phi(x, y) \propto V$$



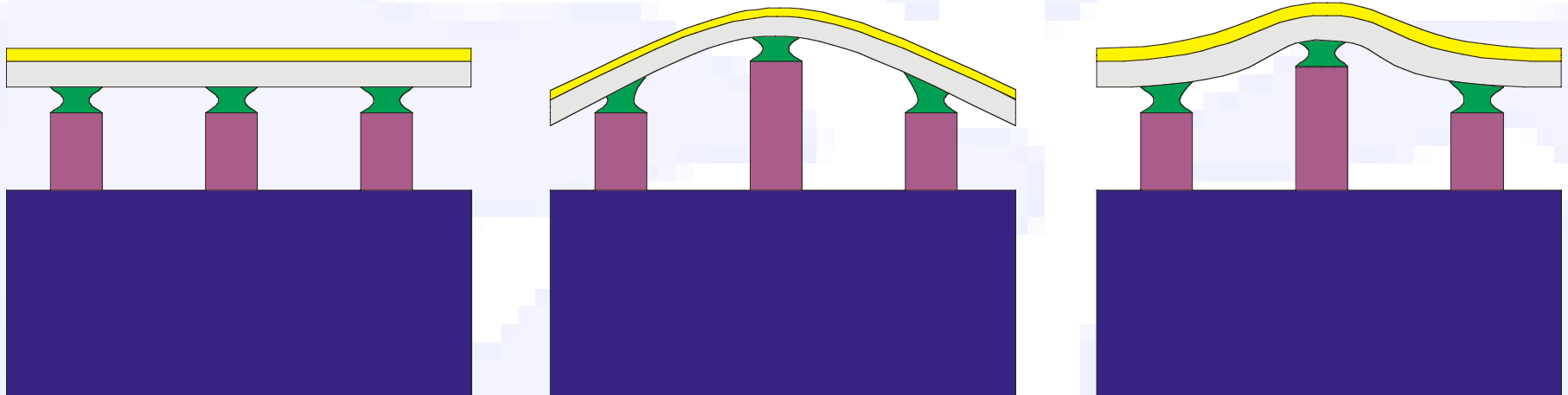
Segmented vs. Continuous

- Continuous
 - High fill factor, “no” diffraction
 - Etch holes and print-through cause diffraction
 - Interactuator coupling
 - Reduced inter-segment stroke
 - Open-loop control more complicated
- Segmented
 - Some diffraction between segments
 - No interactuator coupling
 - High stroke
 - Denser actuator spacing



Influence Function

- Influence function: the shape the mirror will take when pushing one actuator
 - Shape depends on the bending stiffness of the actuators compared to the faceplate stiffness
 - Large influence function (e.g. stiff faceplate) reduces ability to correct



Fitting Error

- Fitting error depends on aberration statistics and mirror type (influence function)
 - Kolmogorov model used for the atmosphere
 - No model for the eye published yet
 - Population studies at U. Indiana, and U. Rochester
 - Doble
- Fitting error (rad²)
 - $a_F = 1.26 P, 0.18 PTT, 0.28 C$
 - Square segments

John W. Hardy, *AO for
Astronomical Telescopes*

$$\sigma_{\text{fit}}^2 = a_F \left(\frac{d}{r_0} \right)^{\frac{5}{3}}$$



Comparing Deformable Mirrors

- Equate the wavefront-fitting errors
- Number of subapertures proportional to d^2

$$\frac{N_1}{N_2} = \left(\frac{d_2}{d_1} \right)^2 = \left(\frac{a_{F1}}{a_{F2}} \right)^{\frac{6}{5}}$$

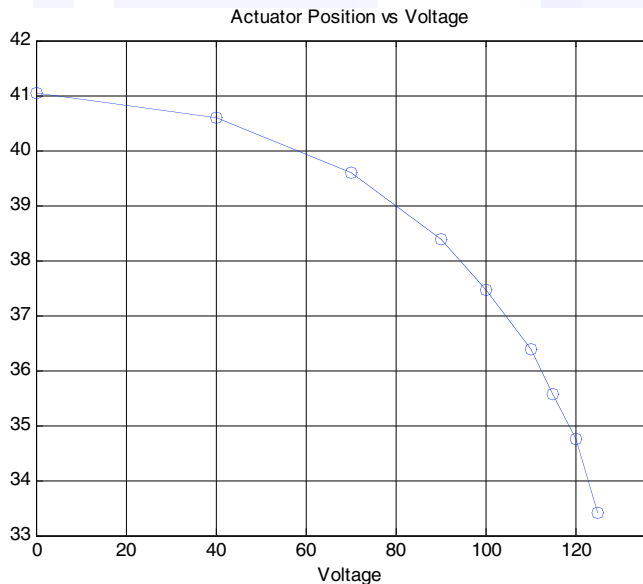
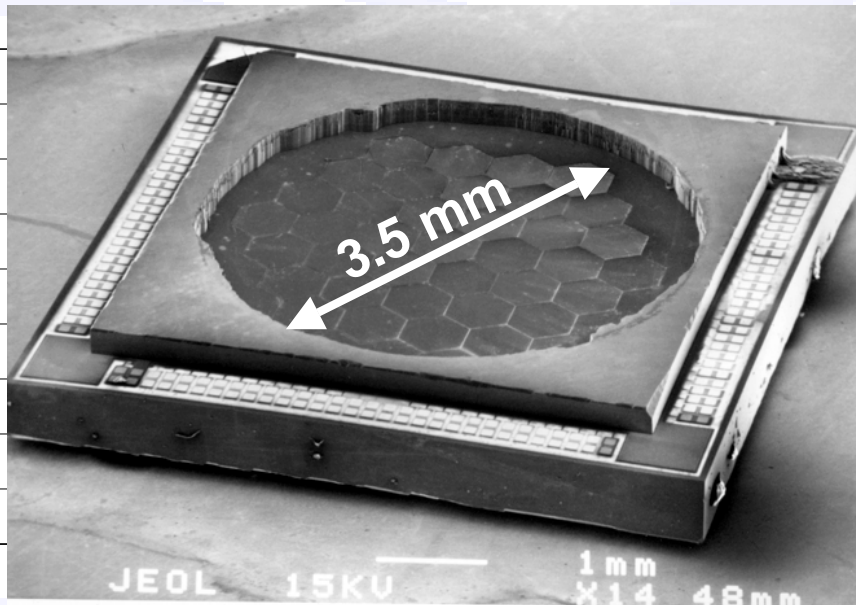
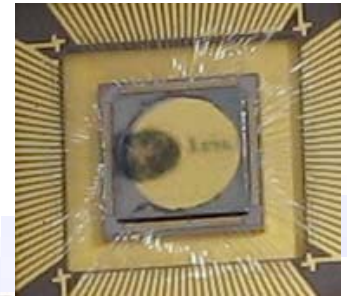
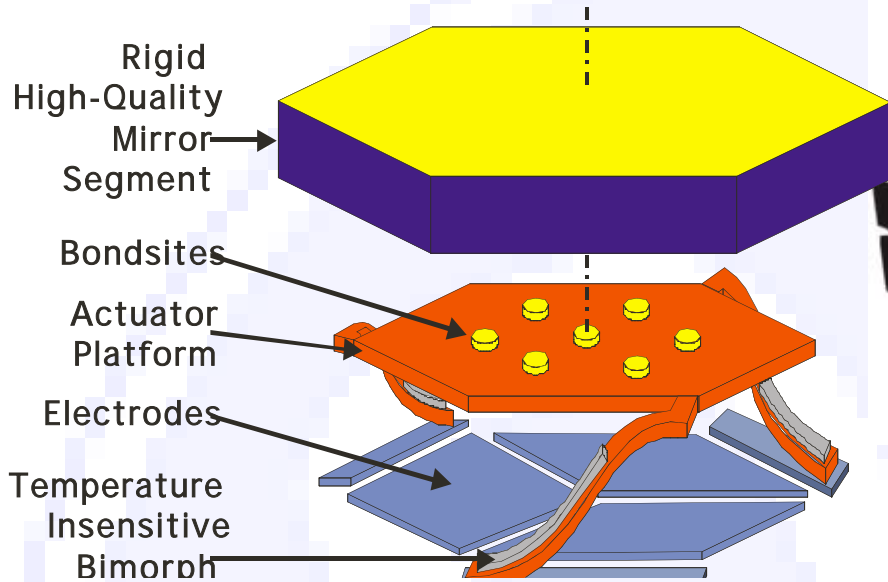
- Subapertures (PTT:C:P) -- 1:1.7:10
- Actuators (PTT:C:P) -- 3:1.7:10



MEMS Deformable Mirrors

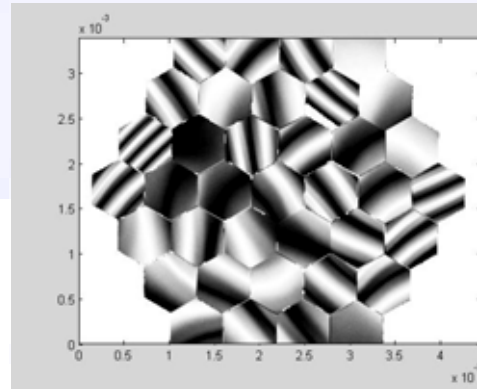
- MEMS (microelectromechanical systems)
 - Based on integrated-circuit fabrication
 - Silicon as a mechanical material
 - Deposit thin films, pattern, etch and repeat (and repeat, and repeat...)
 - High spatial frequencies achievable
 - $d \sim 20\text{-}1000\mu\text{m}$
 - (Potentially) low cost
 - $\sim \$10/\text{actuator}$ compared to $\sim \$1000/\text{actuator}$
 - Scalable to large numbers ($>10,000$) of actuators

Iris AO MEMS Segmented DM

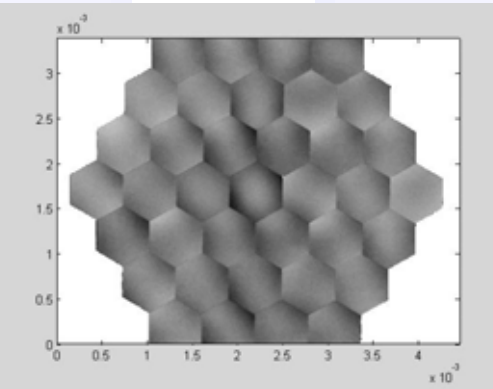


Open-Loop DM Positioning: *Pseudo Fringes* ($\lambda=600\text{ nm}$)

As Released

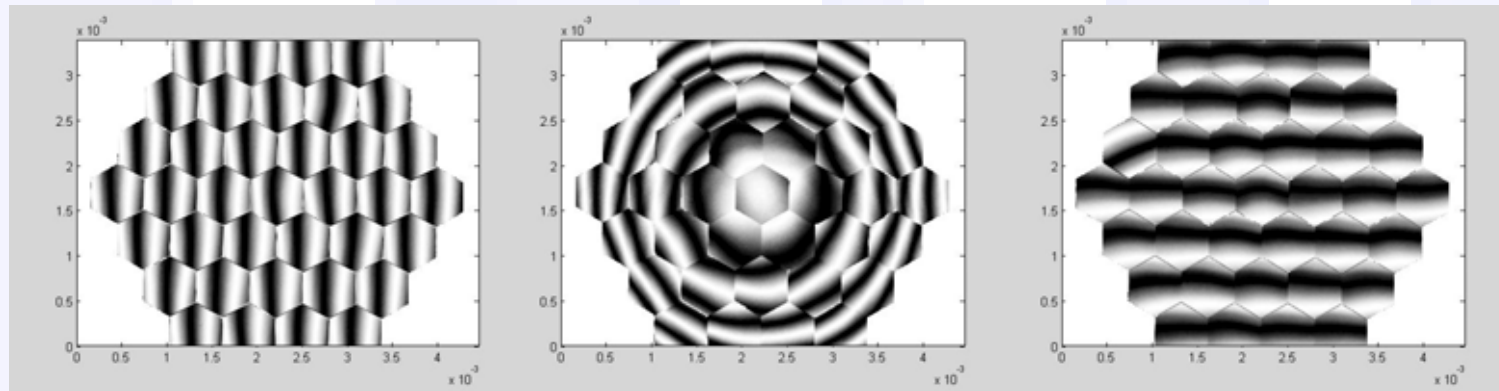


Flattened



Only 19 nm *rms*
residual
wavefront errors

Various Commanded Positions



Hysteresis free actuation enables open-loop positioning



Summary

- DMs change the phase of a wavefront in real time
- DMs can be classified as zonal or modal
 - Continuous and segmented is another classification
- Different types perform differently
 - Match fitting error to compare
- Telescope primary determines DOF and stroke
- MEMS DMs promise to increase DOF and reduce cost