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AO PSF estimation from WFS data on PUEO (CFHT)

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AO PSF Reconstruction Workshop

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Automatic PSF reconstruction

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J.-P. Véran et al., Estimation of the adaptive optics long exposure point spread function using control loop data, Journal of the Optical Society of America A, Vol. 14, No. 11, 1997.

- Implementation: PUEO @ CFHT
- Limitations of the method:
 - Magnitude of guide source ≤ 13.5
 - Kolmogorov model for the high order modes
 - Curvature based AO systems only
- Fundamental limitations:
 - PSF in the direction of the guide star (anisoplanatism)
 - Long exposure PSF only (speckle noise)

Imaging: long exposure PSF

- Long exposure (= infinite integration time) through the atmosphere:

$$\langle PSF(\mathbf{a}) \rangle \propto \langle |FT[\Psi(\mathbf{\check{e}}\mathbf{f})P(\mathbf{\check{e}}\mathbf{f})]^2 \rangle$$

- We recall the near-field approximation: $\Psi(\mathbf{x}) = \exp[i\varphi(\mathbf{x})]$
- We use the autocorrelation formula to compute the long exposure OTF:

$$\langle OTF(\mathbf{f}) \rangle = \langle OTF(\tilde{\mathbf{n}}/\lambda) \rangle = \frac{1}{S} \iint \langle \exp[i\varphi(\mathbf{x}) - i\varphi(\mathbf{x} + \tilde{\mathbf{n}})] P(\mathbf{x})P(\mathbf{x} + \tilde{\mathbf{n}}) d\mathbf{x} \rangle$$

- Gaussian hypothesis:

$$\langle OTF(\mathbf{f}) \rangle = \langle OTF(\tilde{\mathbf{n}}/\lambda) \rangle = \frac{1}{S} \iint D_\varphi(\mathbf{x}, \tilde{\mathbf{n}}) P(\mathbf{x})P(\mathbf{x} + \tilde{\mathbf{n}}) d\mathbf{x}$$

- Kolmogorov model: $D_\varphi(\rho) = \langle |\varphi(\mathbf{x}) - \varphi(\mathbf{x} + \rho)|^2 \rangle = 6.88(\rho/r_0)^{5/3}$

- So we have: $\langle OTF(\mathbf{f}) \rangle = \langle OTF_{atm}(\mathbf{f}) \rangle OTF_{tel}(\mathbf{f})$

where: $\langle OTF_{atm}(\mathbf{f}) \rangle = \exp\left[-\frac{1}{2}D_\varphi(\lambda\mathbf{f})\right] = \exp\left[-3.44(\rho/r_0)^{5/3}\right]$

Separation low order / high order modes

– $\varphi_\varepsilon(\mathbf{r}, t)$ AO corrected wave-front phase

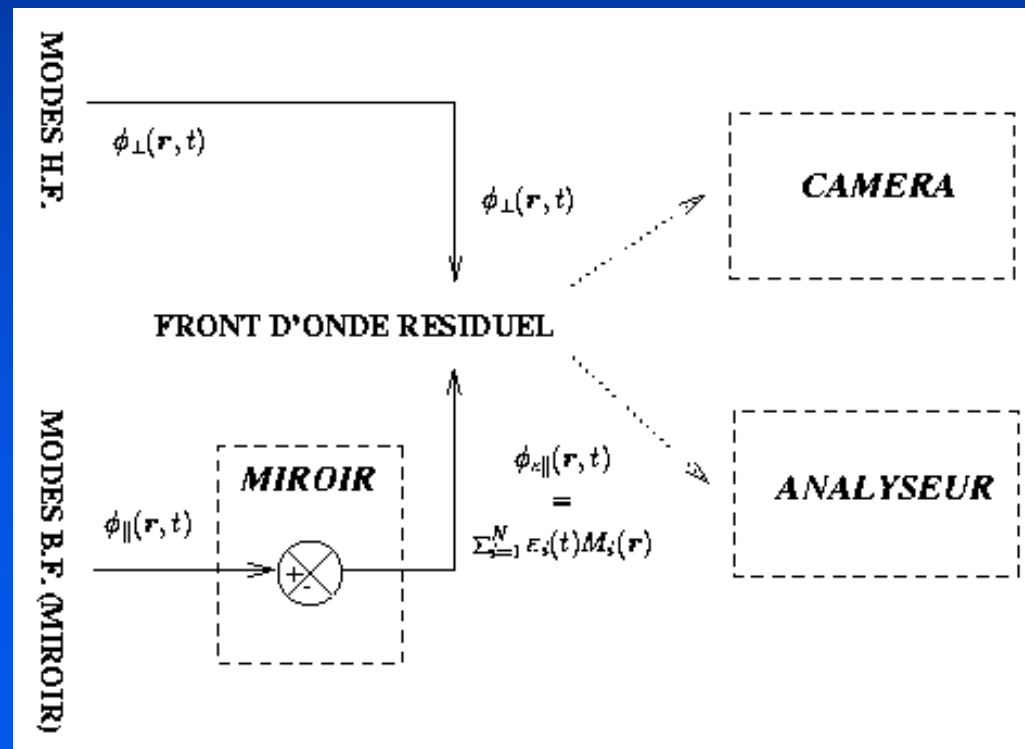
– We have: $\langle OTF_{cor}(\mathbf{f}) \rangle = \exp\left[-\frac{1}{2}D_{\varphi_\varepsilon}(\lambda\mathbf{f})\right] \neq \exp\left[-3.44(\check{e}f / r_0)^{5/3}\right]$

– So we need to estimate: $D_{\varphi_\varepsilon}(\lambda\mathbf{f})$

– We have $\varphi_\varepsilon = \varphi_{\varepsilon\parallel} + \varphi_\perp$
 $\varphi_{\varepsilon\parallel}$ sensed and corrected
 φ_\perp unsensed and uncorrected

– We can show that:

$$D_{\varphi_\varepsilon} = D_{\varphi_{\varepsilon\parallel}} + D_{\varphi_\perp}$$



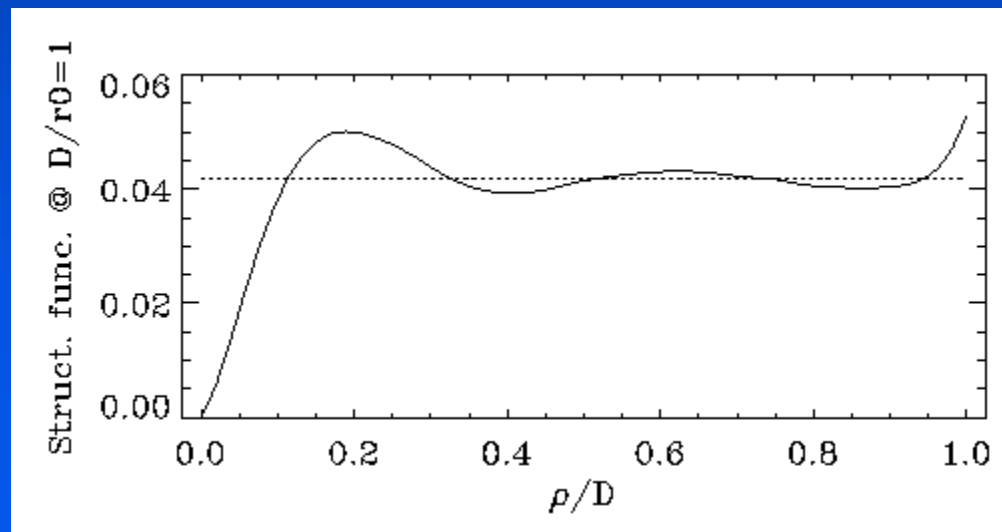
Computation of $D_{\varphi_{\perp}}$

- $D_{\varphi_{\perp}}$ follows the Kolmogorov model and depends only upon r_0

$$D_{\varphi_{\perp}}(\tilde{\mathbf{n}}) = \iint [1 - \cos(2\pi\tilde{\mathbf{n}}\mathbf{k})] PSD_{\varphi_{\perp}}(\mathbf{k}) d\mathbf{k}$$

where:

$$PSD_{\varphi_{\perp}}(\mathbf{k}) = \begin{cases} PSD_{\varphi_{\text{kolmogorov}}}(\mathbf{k}) & \text{if } k > k_M \\ 0 & \text{if } k \leq k_M \end{cases}$$



Computation of $D_{\varphi_{\varepsilon_{\parallel}}}$

– Modal decomposition: $\varphi_{\parallel}(\mathbf{r}, t) = \sum_{i=1}^N \varepsilon_i(t) M_i(\mathbf{r})$

$$D_{\varphi_{\varepsilon_{\parallel}}}(\tilde{\mathbf{n}}) = \sum_{i=1}^N \sum_{j=1}^N \langle \varepsilon_i \varepsilon_j \rangle U_{ij}(\tilde{\mathbf{n}})$$

$$U_{ij}(\tilde{\mathbf{n}}) = \frac{\iint P(\mathbf{x}) P(\mathbf{x} + \tilde{\mathbf{n}}) [M_i(\mathbf{x}) - M_i(\mathbf{x} + \tilde{\mathbf{n}})] [M_j(\mathbf{x}) - M_j(\mathbf{x} + \tilde{\mathbf{n}})] d\mathbf{x}}{\iint P(\mathbf{x}) P(\mathbf{x} + \tilde{\mathbf{n}}) d\mathbf{x}}$$

- $U_{ij}(\tilde{\mathbf{n}})$ can be pre-computed once for all
- We then just need to compute $\langle \varepsilon_i \varepsilon_j \rangle$ for each acquisition we want to get the PSF for.

Computation of $\langle \varepsilon_i \varepsilon_j \rangle$

- If we had a perfect WFS looking at the residual phase, it would measure $\varepsilon_i(t)$ and thus computing $\langle \varepsilon_i \varepsilon_j \rangle$ would be straightforward

- We only have:

$\hat{\varepsilon}_i(t)$	=	$\varepsilon_i(t)$	+	$n_i(t)$	+	$r_i(t)$
Actual WFS measurement		Ideal WFS measurement		Noise on WFS measurement		Spatial aliasing

- If the correction bandwidth is high (fast system, bright guide source):

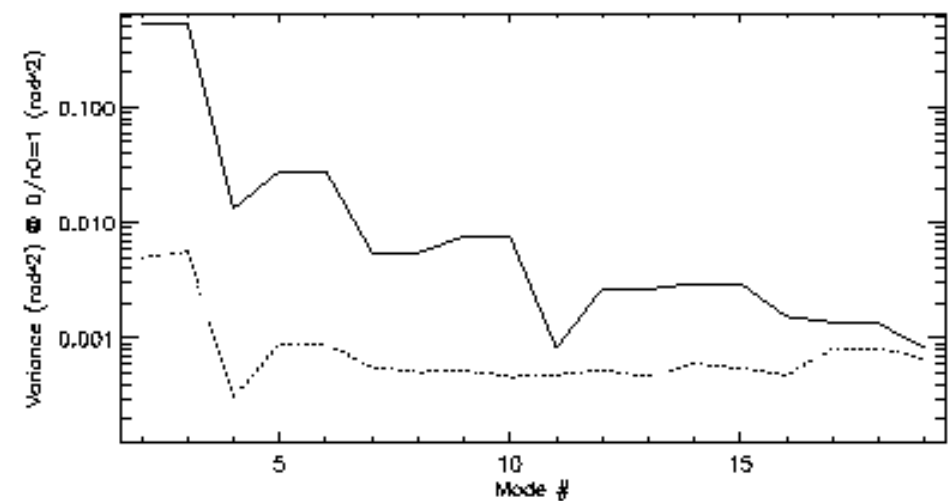
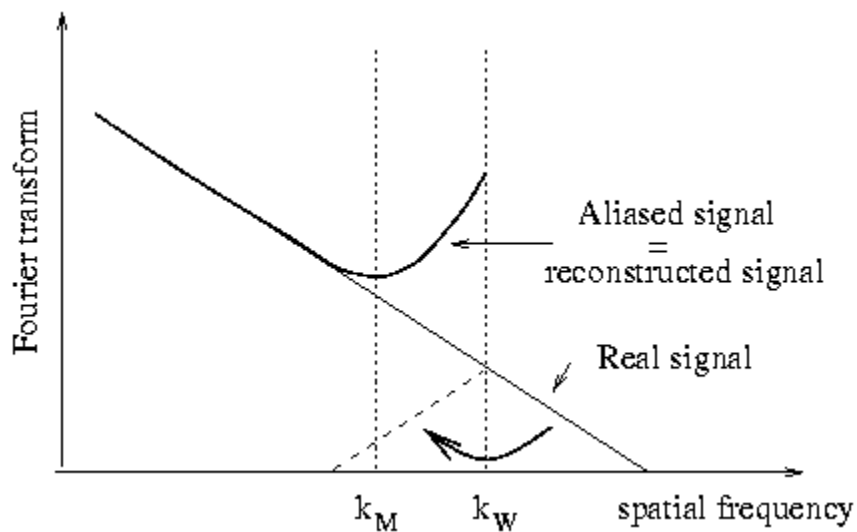
$$\langle \varepsilon_i \varepsilon_j \rangle = \langle \hat{\varepsilon}_i \hat{\varepsilon}_j \rangle - \langle n_i n_j \rangle + \langle r_i r_j \rangle$$

Computation of the spatial aliasing contribution $\langle r_i r_j \rangle$

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- Spatial aliasing is due to finite sampling of the WFS
- Spatial aliasing depends on the type of WFS
- Spatial aliasing depends only on r_0 and can be computed by modeling
- For a curvature WFS, $\sigma_{alias}^2 \approx 1.1\sigma_{fitting}^2$
- For a SH WFS, $\sigma_{alias}^2 \approx 0.3\sigma_{fitting}^2$



Computation of the WFS noise contribution $\langle \hat{\epsilon}_i \hat{\epsilon}_j \rangle - \langle n_i n_j \rangle$

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- WFS noise depends on type of WFS (photon noise, read-out noise, background noise, flat-field, dark current)
- For any WFS operating in closed loop, we have $\sigma_{\hat{\epsilon}_i}^2 \approx \sigma_{n_i}^2$
- Better to compute $\langle \dot{\epsilon}_i \dot{\epsilon}_j \rangle$ where $\dot{\epsilon}_i = \hat{\epsilon}_i - n_i$ (noiseless measurement)
- For curvature sensing, only photon noise (APDs) so:

$$w = \frac{n_1 - n_2}{n_1 + n_2} \quad W = \frac{N_1 - N_2}{N_1 + N_2} \quad n_1 = \text{Poisson}(N_1)$$

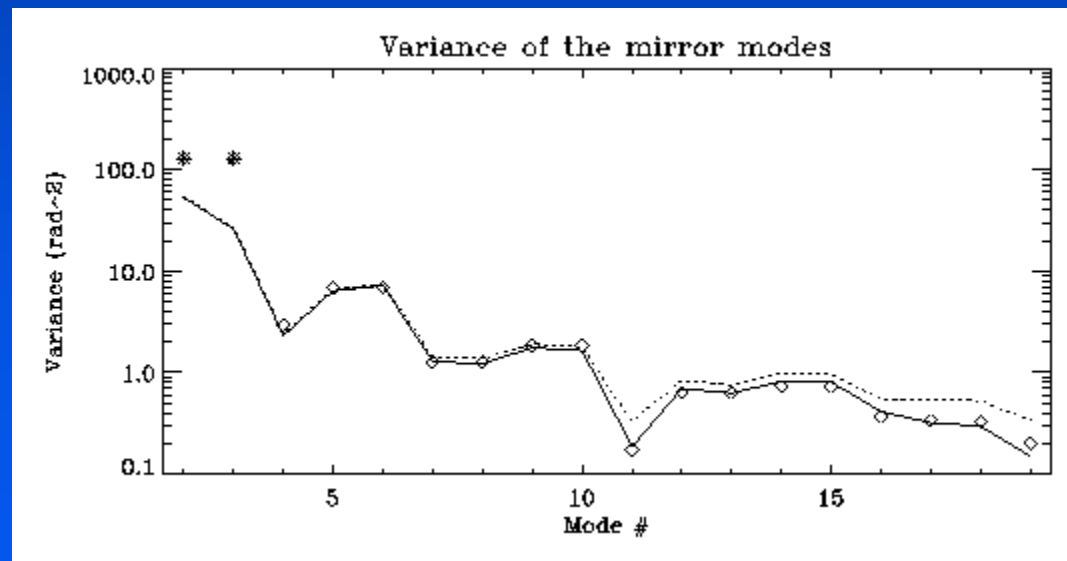
$$n_2 = \text{Poisson}(N_2)$$

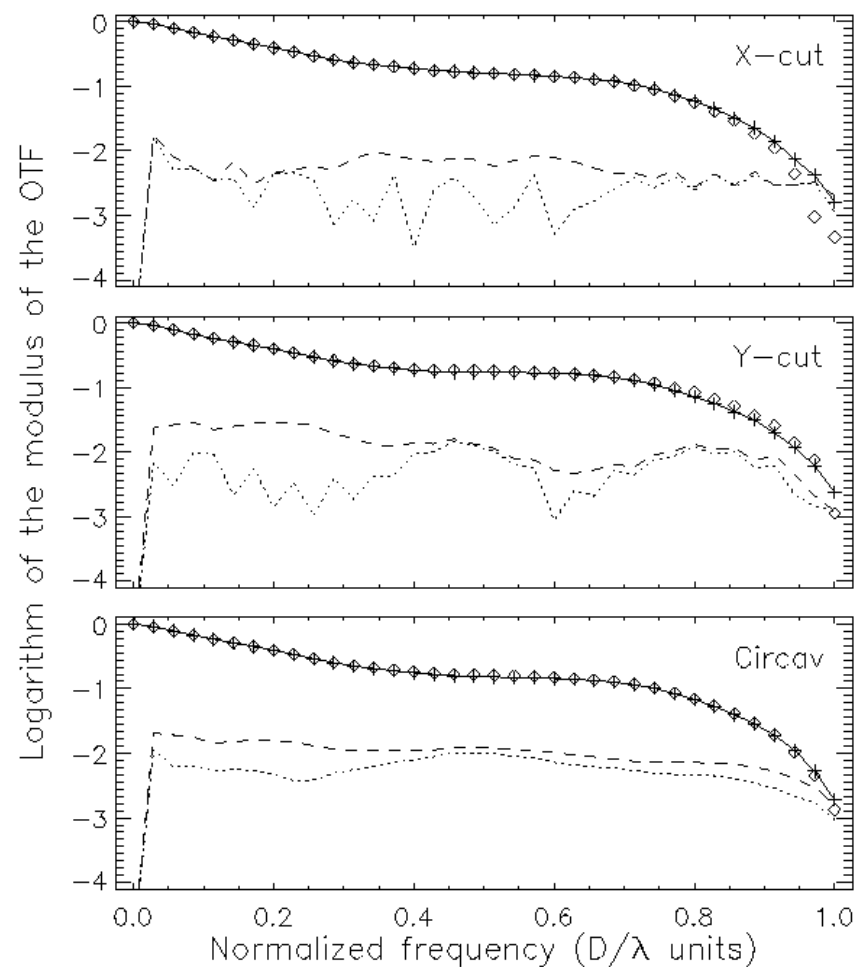
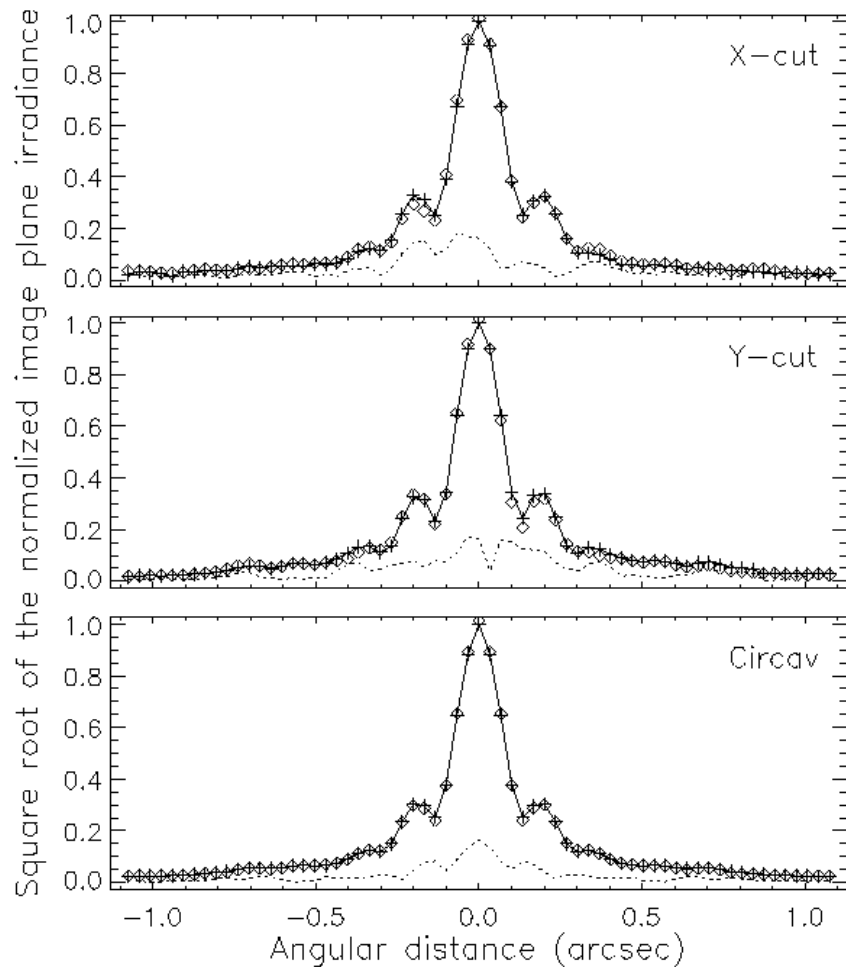
$$\sigma_w^2 = \frac{\sigma^2(n_1 - n_2)}{\langle n_1 + n_2 \rangle}$$

- $n_1 + n_2$ must be large enough

Computation of r_0

- Use external seeing monitor
- or:
- Derive it from the DM command variances (include spatial aliasing and WFS noise).
- Watch for outer scale effect on lowest modes





— & + + Real (measured) PSF

◇ ◇ ◇ ◇ Estimated PSF

..... |Real PSF - Estimated PSF|

G.S.: $m_R = 10.4$

$SR_r = 62.2\%$ $SR_e = 63.6\%$

$r_0 = 15.4\text{cm}$ (@ $0.5\mu\text{m}$)

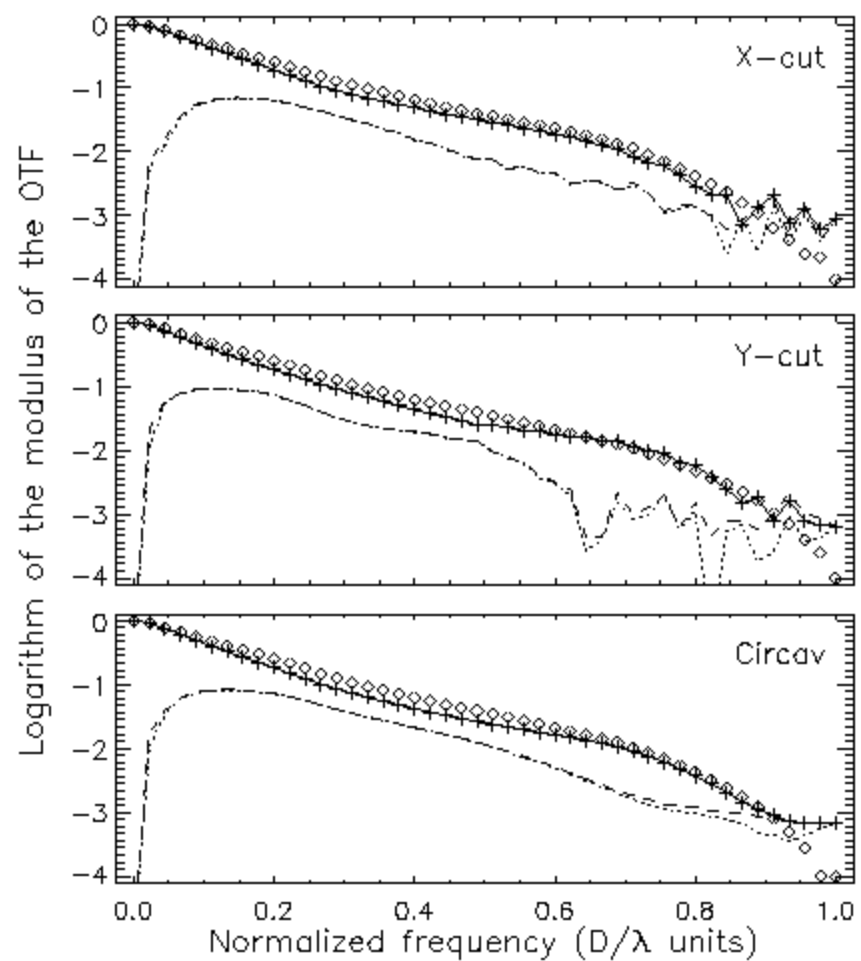
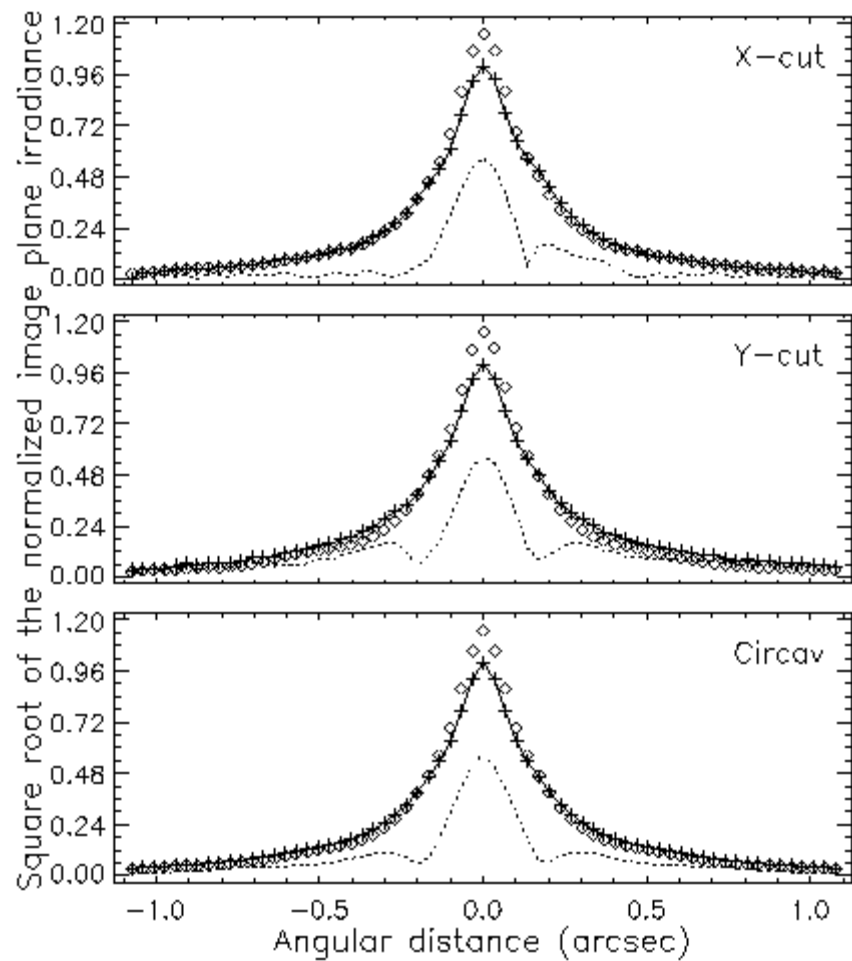
H2 band

— & + + |Real (measured) OTF|

◇ ◇ ◇ ◇ |Estimated OTF|

..... |Real OTF| - |Estimated OTF|

----- |Real OTF - Estimated OTF|



— & + + Real (measured) PSF
 ◇ ◇ ◇ ◇ Estimated PSF
 |Real PSF - Estimated PSF|

G.S.: $m_R = 15.6$
 $SR_r = 16.3\%$ $SRe = 21.6\%$
 $r_0 = 18.5\text{cm}$
 H band

— & + + |Real (measured) OTF|
 ◇ ◇ ◇ ◇ |Estimated OTF|
 |Real OTF| - |Estimated OTF|
 - - - - |Real OTF - Estimated OTF|

Real-time statistics gathering at CFHT

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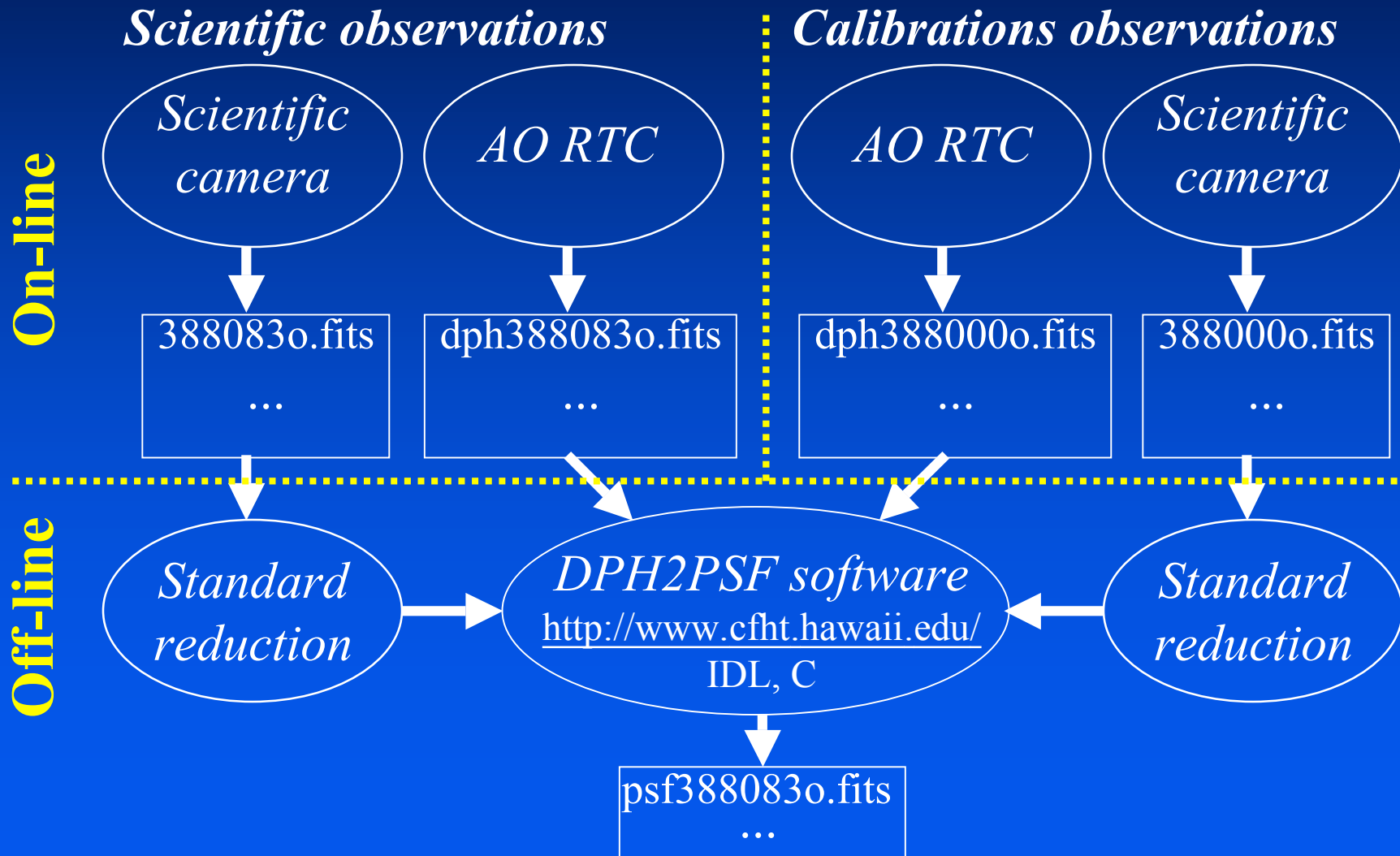
- Statistical data gathered by the AO control computer (SPARC)
- One sample every 30 ms at 1 kHz
- Accumulation starts when exposure starts
- Accumulation stops when exposure stops
- Statistics saved in .psf file
- .psf file analyzed on the fly and structure function is computed (and r0 displayed)
- dphXXXXXX.fits saved with XXXXXXo.fits

```
#PSF Vector of the mean correction modes :  
double PSF_mean_mode_vector = 21 1  
  
#PSF Matrix of the covariances of the correction modes :  
double PSF_covariance_mode_matrix = 21 21  
  
#PSF Vector of the mean actuator controls :  
double PSF_mean_act_ctrl_vector = 21 1  
  
#PSF Matrix of the covariances of the actuator controls :  
double PSF_covariance_act_ctrl_matrix = 21 21  
  
#PSF Vector of the mean APD sum counters :  
double PSF_mean_sum_vector = 19 1  
  
#PSF Vector of the variances of the APD sum counters :  
double PSF_variance_sum_vector = 19 1  
  
#PSF Vector of the mean APD difference counters :  
double PSF_mean_diff_vector = 19 1  
  
#PSF Vector of the variances of the APD difference counters :  
double PSF_variance_diff_vector = 19 1  
  
#PSF Number of count samples during exposure :  
double PSF_count = 1 1  
  
#PSF Vector of the means of the mode gains :  
double PSF_mean_mode_gain_vector = 21 1  
  
#PSF Vector of the variances of the mode gains :  
double PSF_variance_mode_gain_vector = 21 1  
  
#PSF mean optical gain during exposure :  
double PSF_mean_optical_gain = 1 1  
  
#PSF variance optical gain during exposure :  
double PSF_variance_optical_gain = 1 1
```

Procedure @ CFHT

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Optimizations & Diagnostics

NRC CARC
 To DHS and PSF process
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Altair Signal Flow

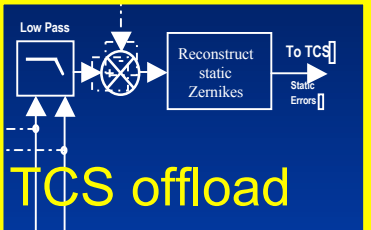
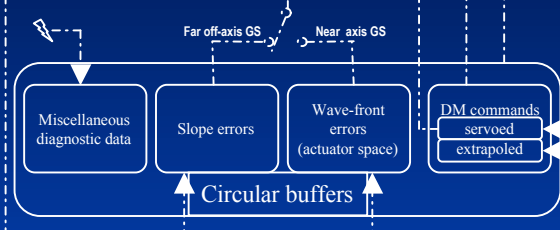
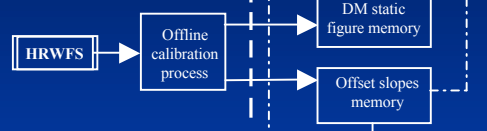
Centroid Gains Optimizer

Modal Gains Optimizer
 Modal Errors Circular Buffer

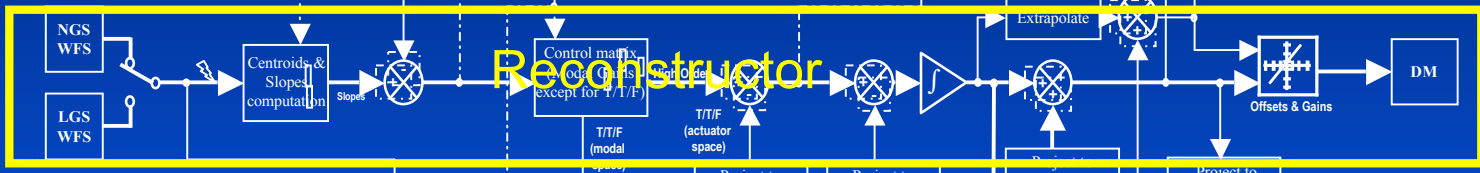
T/T Offloading Gains Optimizer

Statistics Gathering

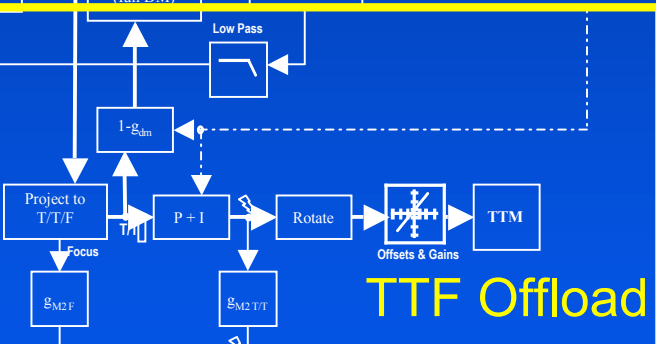
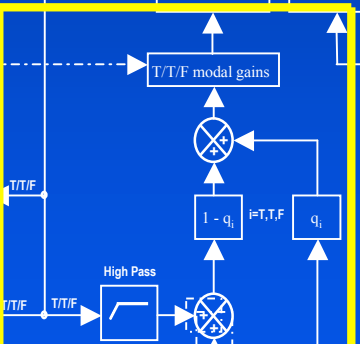
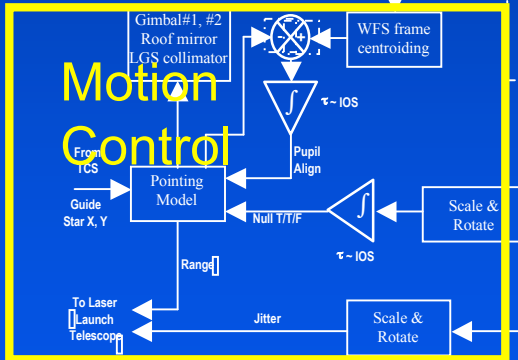
Calibration



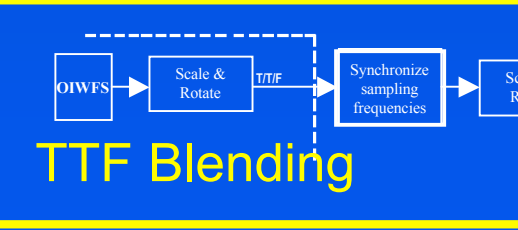
Reconstructor



Motion Control



TTF Blending



Secondary Mirror Control System

WFCS process allocation & major data paths

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